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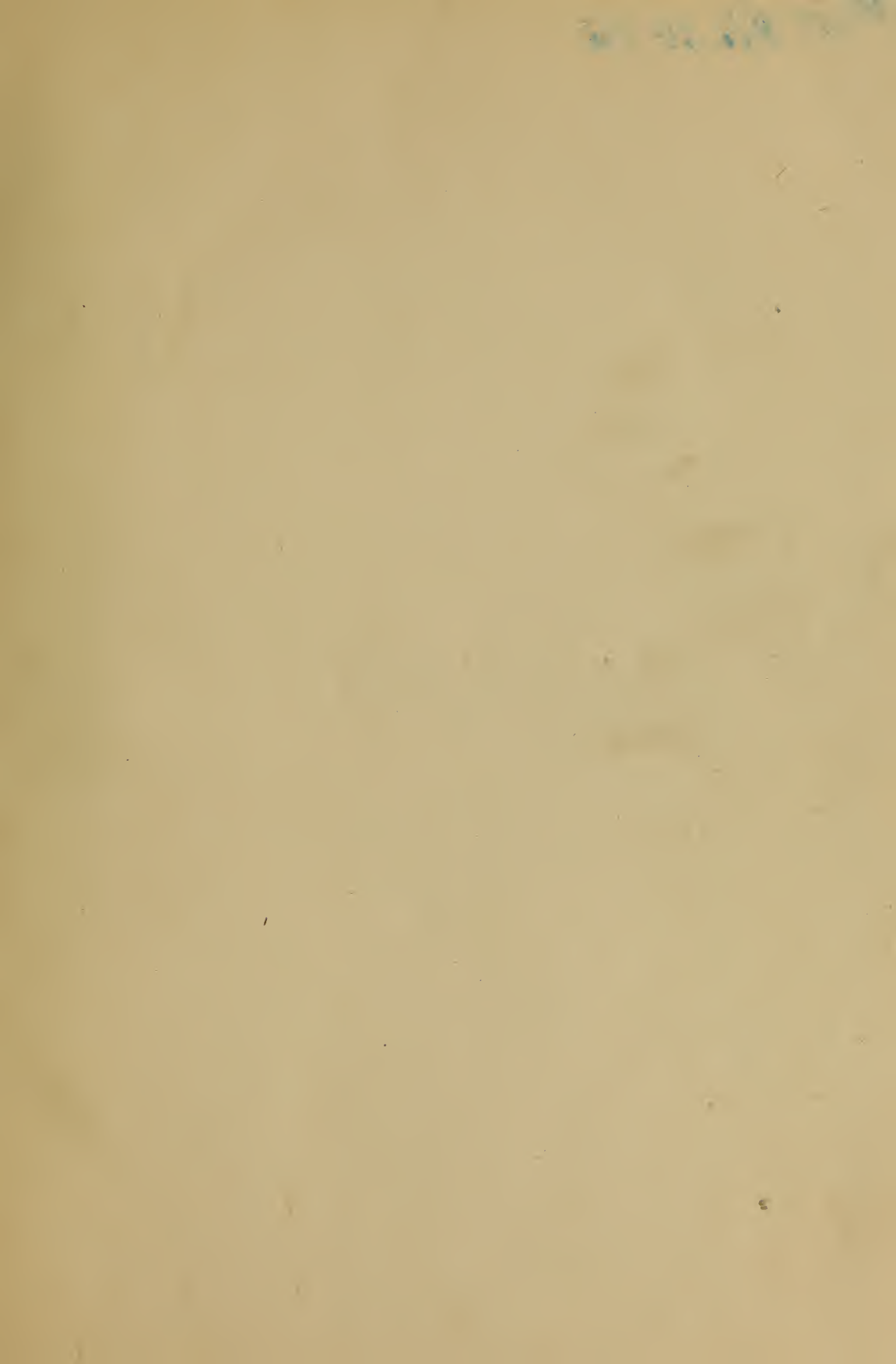


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INFLUENCE OF WAVE FORM ON THE RATE OF INTEGRATING INDUCTION METERS.

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We give in this paper the results obtained with five integrating induction wattmeters, on which we have made a large number of tests, although further work remains to be done. These results may therefore be regarded as preliminary, illustrating the methods employed and the results obtained when changes are made in the wave form by altering the magnitude or phase of the harmonics present.

Two of the meters employed were sent to the Bureau of Standards for test by the makers. The others were meters which we happened to have in the laboratory when the tests were undertaken. The following is a list of the meters:

- No. 1, Stanley (magnetic suspension type), 50 amperes.
- No. 2, Stanley (magnetic suspension type), 50 amperes.
- No. 3, Fort Wayne, type "K," 50 amperes.
- No. 4, General Electric (1902 House type), 25 amperes.
- No. 5, Siemens & Halske, 25 amperes.

All the meters are made for 60 cycles, single phase. The first four are American instruments; the last is of German make. Each meter was tested at full load and at 110 volts, and at approximately unity power factor.

In order to determine the effect on the rate of an induction meter due to varying the wave form, it is necessary to eliminate carefully any effects due to variation in the temperature of the meter or changes in the frequency of current, or other alterations in the conditions of the meter or circuit. In most cases the effect of a moderate distortion of the wave is small, and unless all measurements are made with great care the effects looked for may be masked by other effects or by errors of measurement. The meters were tested alternately with current of sine wave form and with a distorted wave, the distortion being produced by adding a harmonic of three times the frequency

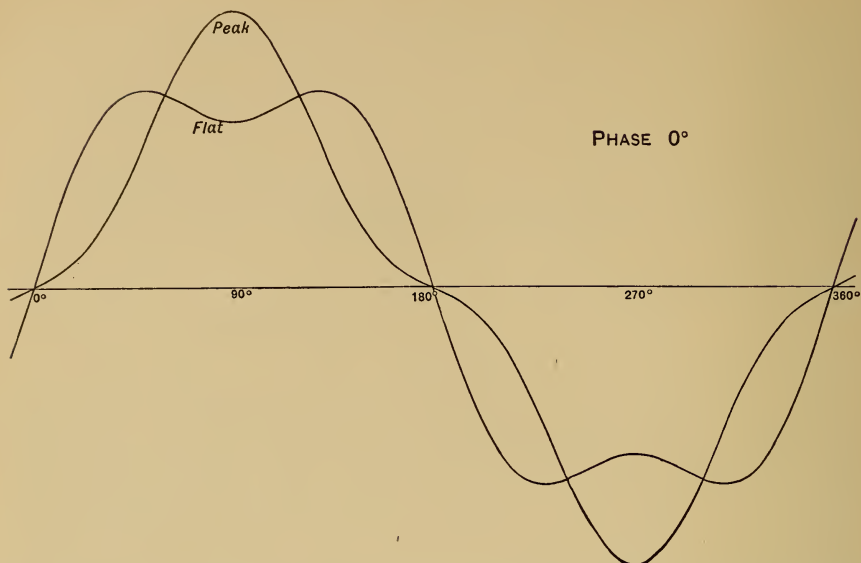


FIG. 1.—Showing the resultant of combining the fundamental and harmonic of three times the frequency and 25 per cent of the magnitude of the fundamental, giving first a peaked wave and second (when the phase of the harmonic is reversed) a flat or dimpled wave. Both fundamental and harmonic are of sine-wave form.

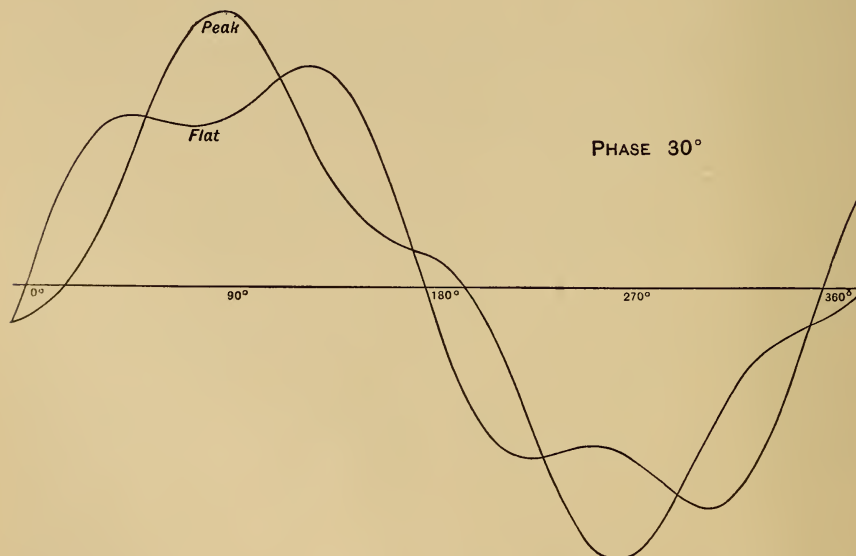


FIG. 2.—Showing the resultant of a fundamental and a harmonic, as in fig. 1, except that the phase of the harmonic has been shifted 30° by changing the coupling 5° .

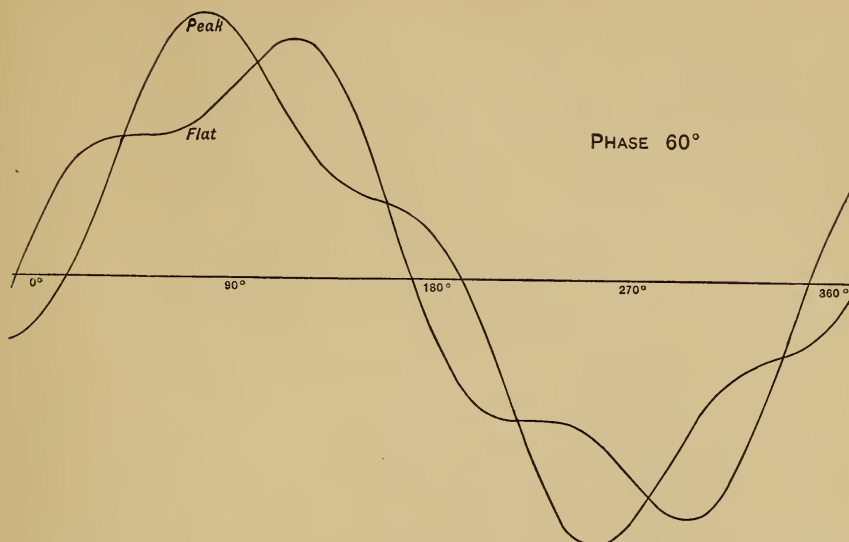


FIG. 3.—Showing the resultant of a fundamental and a harmonic as in fig. 1, except that the phase of the harmonic has been shifted 60° .

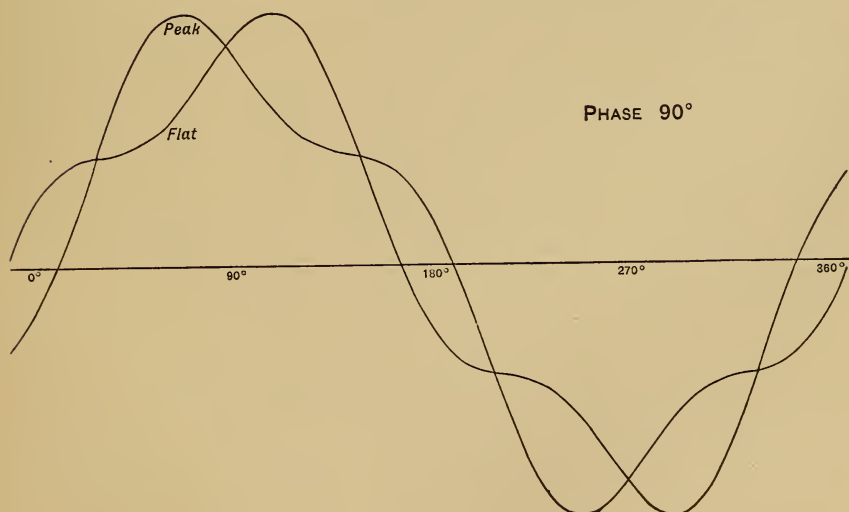


FIG. 4.—Showing the resultant of a fundamental and a harmonic as in fig. 1, except that the phase of the harmonic has been shifted 90° by changing the coupling 15° . The wave form for "peak" and "flat" are here alike, except that the steeper side is in advance in the "peak" and the more gradual slope is in advance on the "flat." "Peak" and "flat" are conventional terms, indicating the phase of the harmonic. If the coupling were shifted 15° more, the "flat" curve would become peaked.

of the fundamental, varying both the amplitude and phase of this harmonic. This was done by means of an alternating current generating set of three machines, two alternators and a direct connected driving motor, one alternator having four poles and the other twelve. The current from each machine is very nearly of sine wave form, and tests were made of the meters alternately with the fundamental only, and with the harmonic added. Three different relative values and four different phases of the harmonic have been employed. The three values of the harmonic are 10 per cent, 25 per cent, and 50 per cent, respectively, of the value of the fundamental. For example, since $E = \sqrt{E_1^2 + E_3^2}$, in the first case the addition of 11 volts of the harmonic to 110 volts of the fundamental gives a resultant of about 110.5 volts, the wave being more or less peaked than a sine wave, according to the phase of the harmonic. In the second case 108 volts of the fundamental plus 27 volts of the harmonic gives a resultant of 111.3 volts. (The voltage in each case was reduced to exactly 110 by resistance in series.) This resultant is shown in figs. 1 to 4, where the 25 per cent harmonic is in different phase in each of the four cases. This difference is produced by shifting the coupling of one of the generators to the driving motor, 5° , 10° , or 15° in the coupling corresponding to 10° , 20° , or 30° in the wave of the fundamental, and to 30° , 60° , or 90° in the phase of the harmonic. A shift of 30° in the coupling corresponds to 180° in the phase of the harmonic, and is the same as reversing the phase by reversing the connections at the terminals of the higher frequency generator. The latter is of course the more convenient, and was the usual method of changing from what we call a flat to a peaked wave. The curves shown in figs. 1 to 4 have been frequently verified by drawing the resultant waves by means of a curve tracer. This not only verifies the wave form, but serves to insure against errors in the connections.

The current, voltage, and power factor, as well as the temperature and frequency, were maintained as nearly constant as possible during a set of runs. A standard wattmeter which was calibrated by direct currents using two potentiometers to measure simultaneously the current and the voltage, was read by a telescope and scale. By means of a carbon rheostat the deflection of this instrument was maintained accurately constant while carrying alternating current during a set of runs on the meters. The wattmeter is of the dynamometer type and astatic. The fixed coils are stranded and wound on wooden spools, and very little metal is used in the region of the coils. The movable coils have very slight inductance, and every precaution is taken to avoid errors due to eddy currents or wave form. The instrument, being

carefully calibrated with direct current, is then correct for alternating current.

Table I.—DETERMINATION OF THE TIMES OF REVOLUTION OF THE DISKS OF THREE METERS.

RUN NO. 1, MAY 26, 1904.

No.	METER 1.			METER 2.			METER 3.				
	Time.	Interval between successive contacts.	Interval between 1st and 15th contacts, 2d and 16th contacts, etc.	Time.	Interval between successive contacts.	Interval between 1st and 15th contacts, 2d and 16th contacts, etc.	Time.	Interval between successive contacts.	Interval between 1st and 15th contacts, 2d and 16th contacts, etc.		
	<i>m.</i> <i>s.</i>			<i>m.</i> <i>s.</i>			<i>m.</i> <i>s.</i>				
1	1 5.30	1.55		0 45.96	1.60		0 45.70	1.30			
2	6.85	1.55		47.56	1.68		47.00	1.31			
3	8.40	1.65		49.24	1.57		48.31	1.32			
4	10.05	1.61		50.81	1.61		49.63	1.37			
5	11.66	1.64		52.42	1.63		51.00	1.30			
6	13.30	1.52		54.05	1.54		52.30	1.30			
7	14.82	1.63		55.59	1.66		53.60	1.37			
8	16.45	1.60		57.25	1.65		54.97	1.33			
9	18.05	1.67		58.90	1.60		56.30	1.30			
10	19.72	1.58		1 0.50	1.55		57.60	1.40			
11	21.30	48.60		2.05	48.25		59.00	26.60			
12	2 9.90	32.20		50.30	32.10		1 25.60	39.88			
13	42.10	32.22		2 22.40	32.10		2 5.48	39.87			
14	3 14.32	32.33		54.50	32.20		45.35	39.95			
15	46.65	1.55	161.35	3 26.70	1.65	160.74	3 25.30	1.30	159.60		
16	48.20	1.62	161.35	28.35	1.60	160.79	26.60	1.30	159.60		
17	49.82	1.59	161.42	29.95	1.59	160.71	27.90	1.30	159.59		
18	51.41	1.59	161.36	31.54	1.56	160.73	29.20	1.35	159.57		
19	53.00	1.61	161.34	33.10	1.68	160.68	30.55	1.40	159.55		
20	54.61	1.61	161.31	34.78	1.60	160.73	31.95	1.35	159.65		
21	56.22	1.68	161.40	36.38	1.62	160.79	33.30	1.33	159.70		
22	57.90	1.58	161.45	38.00	1.60	160.75	34.63	1.32	159.66		
23	59.48	1.55	161.43	39.60	1.59	160.70	35.95	1.40	159.65		
24	4 1.03	1.59	161.31	41.19	1.61	160.69	37.35	1.33	159.75		
25	2.62		161.32	42.80		160.75	38.68		159.68		
Mean time for 100 revolutions			161.367	Mean time for 100 revolutions			160.733	Mean time for 120 revolutions			159.636
Time in seconds for one revolution.....			1.6137	Time in seconds for one revolution			1.6073	Time in seconds for one revolution.....			1.3303

DETERMINATION OF THE RATE OF THE METERS AND THE FREQUENCY OF THE CURRENT.

The rate of the meters was determined by means of a chronograph and chronometer, record being made at the end of every revolution of the disk or drum for the first ten revolutions at the beginning of a

run and the last ten at the end of the run, and in addition once in ten or twenty revolutions during the run. The runs average about three minutes each. The record on the chronograph sheet was read by means of a diagonal scale and gave the mean time of one revolution with great accuracy. An example is given in Table I. Eleven independent determinations of the time of 100 revolutions of the disk are given in the fourth and seventh columns for meters 1 and 2 and of 120 revolutions in the tenth column for meter 3. The average of these eleven values is used in deriving the mean time for one revolution. At the same time an electric circuit was closed by a contact point connected to the generator once in every hundred revolutions, and these contacts were recorded on the chronograph sheet. This gave the frequency of the current very exactly. A slight correction is applied to the rate of each meter for the small departure of the frequency from 60, which is the standard frequency for the meters tested. This correction is of course determined for each meter separately and may be taken from the curves in fig. 10. In Table II are given the readings from the chronograph record for determining the frequency of the current, which in this case averaged 59.95 for the period of the run.

Table II.—RECORD FOR DETERMINATION OF THE FREQUENCY OF THE CURRENT.

Time of contacts at beginning of run.		Time of contacts at end of run.	Time for 5,100 revolutions.
<i>m.</i>	<i>s.</i>	<i>m.</i> <i>s.</i>	<i>Seconds.</i>
1	3.25	3 53.40	170.15
	6.60		170.13
	9.92	4 0.05	170.13
	13.28		170.12
	16.60		170.15

Mean = 170.136

$$\text{Frequency} = \frac{2 \times 5,100}{170.136} = 59.95 \text{ cycles per second.}$$

Before making a series of runs on the meters the load was applied and they were warmed up to an equilibrium temperature. In order to eliminate errors due to any changes in temperature that might subsequently occur, as well as any other constant errors due to changing conditions, and so obtain the effect of the varying wave form alone, the tests with distorted wave forms were interspersed with tests using sine wave forms. Any progressive change in the meters, or the standard wattmeter, would thus be eliminated. Table III gives the

results of 49 runs on three meters made May 26, 1904, using a sine wave and a distorted wave due to 25 per cent harmonic, peak and flat, as shown in figs. 1 to 4. The numbers of the runs show the order in which they were taken. For example, the first, fourth, and seventh were made with a sine wave and are grouped together in the table. The actual frequency for each run is given in the table, but the times of one revolution given in columns 6, 8, and 10 have been reduced to 60 cycles. The numbers given in columns 7, 9, and 11 are the means of the corresponding values in columns 6, 8, and 10.

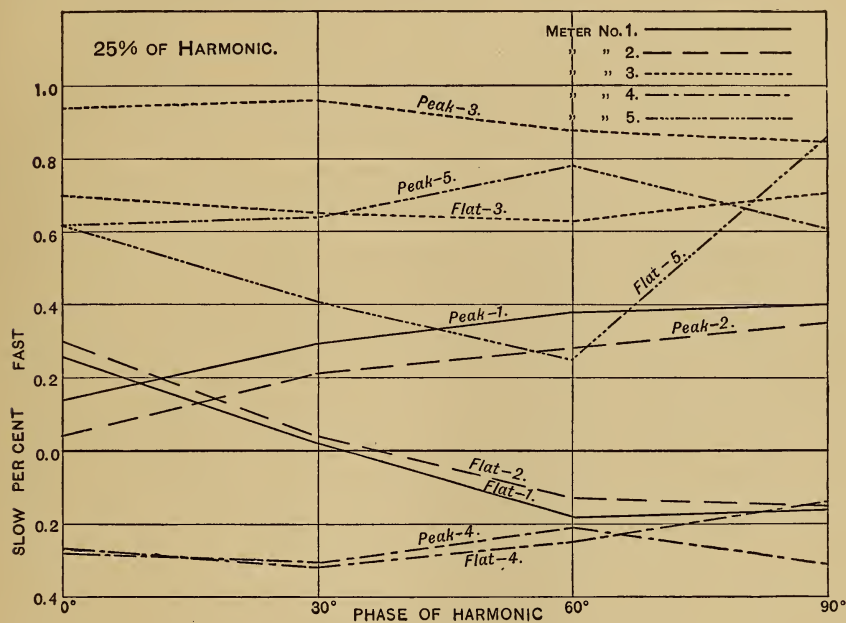


FIG. 5.—Showing the variation in the rate of five induction meters with 25 per cent harmonic in the current as the phase of the harmonic is changed from 0° to 30° , 60° , and 90° .

Runs 2 and 5 were made using a peaked wave and runs 3 and 6 using a flat wave. The phase of the harmonic was then shifted 30° , and seven runs made in the same order as before. The third set of seven runs was made with the harmonic at 60° , the fourth set at 90° , and then three more sets of runs were made in reverse order with respect to the phase of the harmonic, making in all seven sets of seven runs each. The difference in per cent obtained in Table IV, together with corresponding differences in other runs using 10 and 50 per cent harmonic, the detailed results of which are not here given, are shown in Table V. All these results are plotted in figs. 5 to 9. The results obtained in the runs of May 26, given in Tables III and IV, are plotted in fig. 5.

Table III.—TABLE OF RESULTS OF 49 RUNS ON THREE METERS USING SINE, PEAK AND FLAT WAVES, WITH DIFFERENT PHASES OF THE HARMONIC, WHICH IS 25 PER CENT OF THE FUNDAMENTAL.

No. of run.	Phase of harmonic.	Lag of current.	Wave form.	Frequency.	Time in seconds for one revolution of disk.					
					Meter No. 1.		Meter No. 2.		Meter No. 3.	
					Time.	Mean.	Time.	Mean.	Time.	Mean.
1	19.8	Sine	59.95	1.6137	} 1.6154	1.6073	} 1.6084	1.3303	} 1.3308
4	18.9	Sine	60.35	1.6178		1.6109		1.3321	
7	18.6	Sine	60.23	1.6148		1.6071		1.3300	
2	0	19.8	Peak ...	59.89	1.6180	} 1.6183	1.6093	} 1.6099	1.3438	} 1.3431
5	0	19.0	Peak ...	60.31	1.6187		1.6105		1.3425	
3	0	17.0	Flat	60.38	1.6203	} 1.6193	1.6141	} 1.6131	1.3407	} 1.3398
6	0	Flat	60.26	1.6184		1.6121		1.3390	
8	Sine	59.96	1.6121	} 1.6148	1.6051	} 1.6077	1.3289	} 1.3305
11	20.0	Sine	60.08	1.6169		1.6099		1.3320	
14	19.2	Sine	59.95	1.6153		1.6082		1.3307	
9	30	19.1	Peak ...	60.09	1.6197	} 1.6199	1.6116	} 1.6120	1.3440	} 1.3441
12	30	19.3	Peak ...	59.98	1.6202		1.6125		1.3443	
10	30	17.7	Flat	60.12	1.6149	} 1.6152	1.6091	} 1.6092	1.3405	} 1.3404
13	30	17.0	Flat	59.99	1.6155		1.6092		1.3404	
15	19.5	Sine	60.14	1.6148	} 1.6156	1.6089	} 1.6088	1.3309	} 1.3309
18	18.9	Sine	60.04	1.6158		1.6086		1.3306	
21	18.3	Sine	59.90	1.6162		1.6088		1.3311	
16	60	17.9	Peak ...	60.10	1.6214	} 1.6216	1.6127	} 1.6133	1.3423	} 1.3426
19	60	17.2	Peak ...	60.12	1.6219		1.6140		1.3429	
17	60	16.6	Flat	60.05	1.6127	} 1.6126	1.6063	} 1.6061	1.3393	} 1.3391
20	60	15.9	Flat	59.94	1.6125		1.6059		1.3390	
22	20.2	Sine	60.28	1.6151	} 1.6151	1.6076	} 1.6079	1.3302	} 1.3305
25	Sine	60.10	1.6152		1.6084		1.3307	
28	19.8	Sine	60.05	1.6150		1.6077		1.3306	
23	90	18.9	Peak ...	60.18	1.6211	} 1.6216	1.6133	} 1.6136	1.3417	} 1.3419
26	90	18.3	Peak ...	60.07	1.6222		1.6138		1.3422	
24	90	18.0	Flat	60.10	1.6124	} 1.6125	1.6056	} 1.6054	1.3401	} 1.3400
27	90	Flat	60.04	1.6127		1.6052		1.3399	
29	19.3	Sine	59.86	1.6162	} 1.6178	1.6091	} 1.6103	1.3322	} 1.3328
32	19.1	Sine	60.15	1.6183		1.6105		1.3328	
35	19.3	Sine	60.11	1.6190		1.6113		1.3333	

Table III.—TABLE OF RESULTS OF 49 RUNS ON THREE METERS USING SINE, PEAK AND FLAT WAVES, ETC.—Continued.

No. of run.	Phase of harmonic.	Lag of current.	Wave form.	Frequency.	Time in seconds for one revolution of disk.					
					Meter No. 1.		Meter No. 2.		Meter No. 3.	
					Time.	Mean.	Time.	Mean.	Time.	Mean.
30	60	18.1	Peak ...	59.83	1.6234	} 1.6239	1.6145	} 1.6150	1.3447	} 1.3448
33	60	Peak ...	60.11	1.6244		1.6154		1.3450	
31	60	16.8	Flat	60.22	1.6143	} 1.6149	1.6087	} 1.6089	1.3405	} 1.3414
34	60	16.3	Flat	60.10	1.6155		1.6091		1.3423	
36	20.0	Sine	60.12	1.6184	} 1.6179	1.6116	} 1.6108	1.3339	} 1.3332
39	20.1	Sine	60.20	1.6177		1.6103		1.3330	
41	20.1	Sine	60.25	1.6176		1.6104		1.3326	
37	30	19.5	Peak ...	60.12	1.6222	} 1.6220	1.6132	} 1.6132	1.3457	} 1.3455
40	30	Peak ...	60.22	1.6219		1.6131		1.3454	
38	30	17.5	Flat	60.17	1.6169	} 1.6182	1.6104	} 1.6110	1.3414	} 1.3415
42	30	Flat	60.27	1.6195		1.6115		1.3417	
44	20.2	Sine	1.6178	} 1.6177	1.6101	} 1.6106	1.3326	} 1.3327
47	20.4	Sine	60.01	1.6176		1.6112		1.3328	
45	0	Peak	1.6191	} 1.6190	1.6104	} 1.6106	1.3453	} 1.3456
49	0	22.0	Peak ...	60.11	1.6190		1.6107		1.3460	
43	0	Flat	1.6216	} 1.6220	1.6154	} 1.6154	1.3424	} 1.3426
46	0	17.6	Flat	60.04	1.6224		1.6154		1.3429	

Table IV.—SUMMARY OF RESULTS SHOWN IN TABLE III.

Meter No.	Phase of harmonic.	Sine.	Peak.	Per cent slow.	Flat.	Per cent.	
						Slow.	Fast.
1	0	1.6166	1.6186	0.12	1.6206	0.25
1	30	1.6164	1.6210	0.28	1.6167	0.02
1	60	1.6167	1.6228	0.38	1.6138	0.18
1	90	1.6151	1.6216	0.40	1.6125	0.16
2	0	1.6095	1.6102	0.04	1.6142	0.29
2	30	1.6092	1.6126	0.21	1.6101	0.06
2	60	1.6096	1.6142	0.29	1.6075	0.13
2	90	1.6079	1.6136	0.35	1.6054	0.16
3	0	1.3318	1.3444	0.95	1.3412	0.70
3	30	1.3318	1.3448	0.98	1.3410	0.69
3	60	1.3318	1.3437	0.89	1.3402	0.63
3	90	1.3305	1.3419	0.85	1.3400	0.71

In Table IV the values given are the means of the two values found for the corresponding case and shown in Table III. Thus 1.6166 is the average of 1.6154, the mean found for runs 1, 4, 7 and

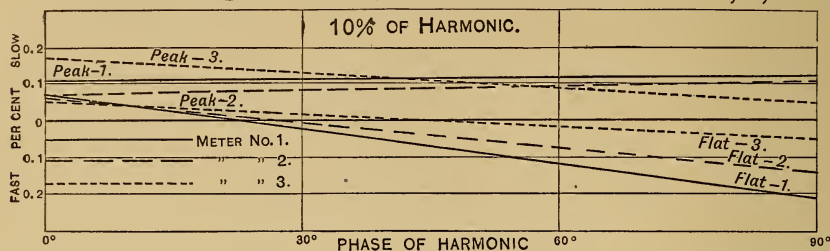


FIG. 6.—Showing the variation in the rate of three induction meters with 10 per cent harmonic in the current as the phase of the harmonic is changed from 0° to 90° .

1.6177, the mean of runs 44, 47. Likewise, 1.6186 is the average of 1.6183 (runs 2, 5) and 1.6190 (runs 45, 49). This eliminates effect of changing temperature during the course of the experiments.

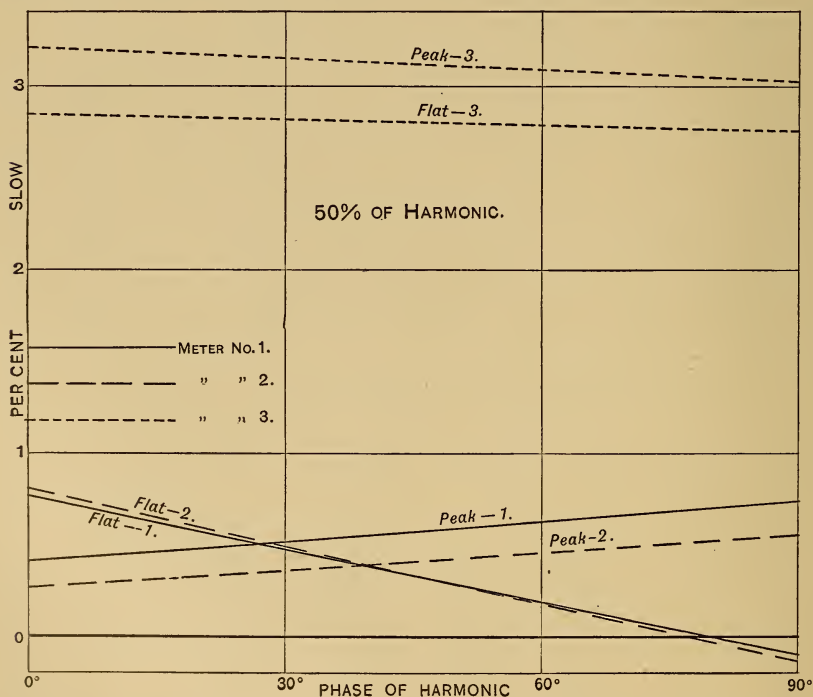


FIG. 7.—Showing the variation in the rate of three induction meters with 50 per cent harmonic in the current as the phase of the harmonic is changed from 0° to 90° .

The maximum variation due to 25 per cent harmonic is, in the case of meter 3, a little less than 1 per cent, being greater with the peak than the flat, but not varying much with the phase of the

harmonic. On the other hand, meters 1 and 2 show smaller errors due to the presence of the harmonic, but greater changes due to shifting the phase of the harmonic, both changing from slow to fast on the flat wave when the phase is shifted. Meter 4 runs faster for both peak and flat and at all phases than on a sine wave. It is the only meter of the five for which this is true.

Fig. 6 shows the effect of changing the phase of the harmonic from 0° to 90° when using a harmonic of 10 per cent, and fig. 7 shows the same for 50 per cent. Only three meters were used in these experiments.

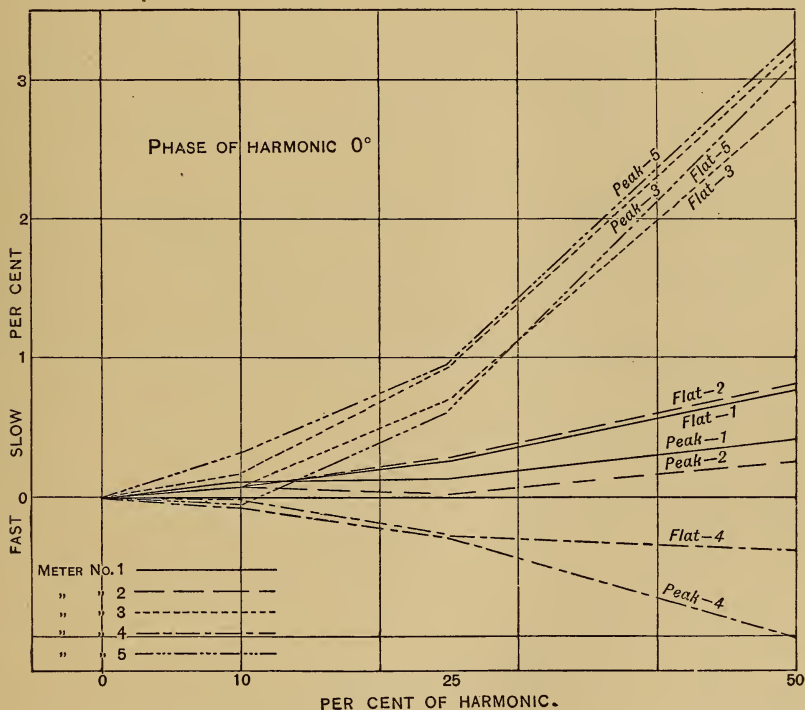


FIG. 8.—Showing the variation in the rate of five induction meters with 10, 25, and 50 per cent of harmonic, the phase of the harmonic in each case being 0° .

Fig. 8 shows the effect of changing the harmonic from 10 per cent to 25 per cent and 50 per cent, keeping the phase constant. Meters 1 and 2 show the least change in rate; meter 4 runs faster, and meters 3 and 5 run slower and show the greatest change in rate. Fig. 9 shows for three meters the same thing as fig. 8, except that the phase of the harmonic is 90° different. Meters 1 and 2 show relatively small changes, but both run faster on the flat than on the sine. Meter 3 runs nearly 3 per cent slower on the 50 per cent harmonic than on the sine.

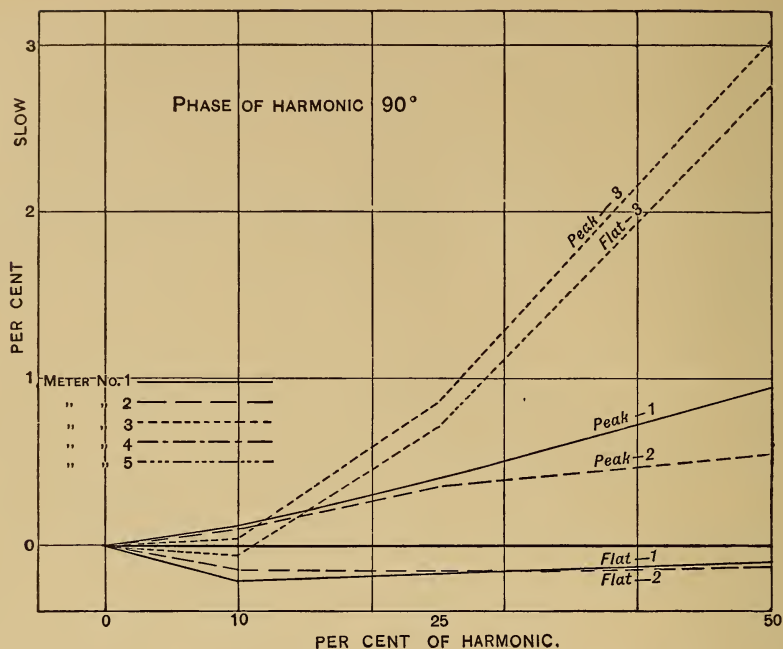


FIG. 9.—Showing the variation in the rate of three induction meters with 10, 25, and 50 per cent of harmonic, the phase of the harmonic in each case being 90° .

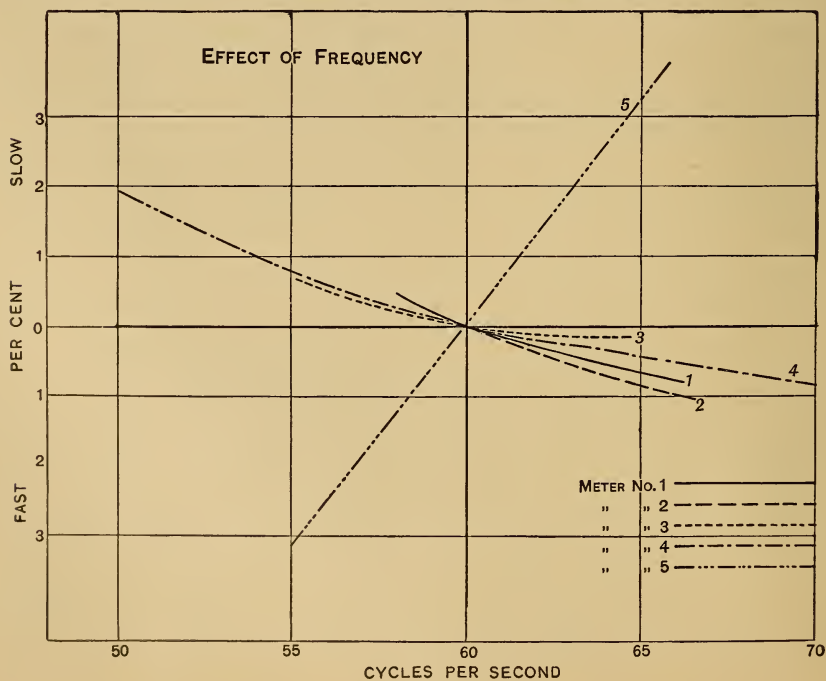


FIG. 10.—Showing the variation in the rate of five induction meters with change of frequency.

Table V.—EFFECT OF VARYING THE PHASE OF THE HARMONIC.

[Change of rate of meters in per cent.]

Percentage of harmonic.	Phase 0°.			Phase 30°.			Phase 60°.			Phase 90°.		
	Flat.		Peak.	Flat.		Peak.	Flat.		Peak.	Flat.		Peak.
	Fast.	Slow.	Fast. Slow.	Fast.	Slow.	Fast. Slow.	Fast.	Slow.	Fast. Slow.	Fast.	Slow.	Fast. Slow.
<i>10 per cent harmonic.</i>												
Meter No. 1.....	0.07	0.11	0.21	0.12
Meter No. 2.....	0.06	0.07	0.14	0.11
Meter No. 3.....	0.05	0.17	0.05	0.05
Meter No. 4.....	0.01	0.07
Meter No. 5.....	0.05	0.32
<i>25 per cent harmonic.</i>												
Meter No. 1.....	0.25	0.12	0.02	0.28	0.18	0.38	0.16	0.40
Meter No. 2.....	0.29	0.04	0.06	0.21	0.13	0.29	0.16	0.35
Meter No. 3.....	0.70	0.95	0.69	0.98	0.63	0.89	0.71	0.85
Meter No. 4.....	0.27	0.28	0.32	0.31	0.25	0.23	0.14	0.31
Meter No. 5.....	0.62	0.95	0.41	0.64	0.25	0.78	0.86	0.61
<i>50 per cent harmonic.</i>												
Meter No. 1.....	0.77	0.41	0.10	0.74
Meter No. 2.....	0.81	0.26	0.13	0.55
Meter No. 3.....	2.84	3.21	2.75	3.03
Meter No. 4.....	0.39	1.01
Meter No. 5.....	3.10	3.26

The effect of change of frequency on the rate of the meters is shown in fig. 10. It is relatively small in every case but one.

These results show that with suitable precautions induction meters may be made to repeat their readings very accurately, so that precision methods may be applied in studying them. They also show that the variations due to wave form depend not only on the harmonics which are present and their magnitudes, but also on their phases.

The Bureau of Standards is now having a generating set constructed which will give all the odd harmonics up to the fifteenth and any desired combination of them with the fundamental. When this is completed it will be used to study the effects of the higher harmonics on the rate of these meters. The results given here show that for commercial purposes all the meters so far studied may be considered accurate on any ordinary wave form where only the third harmonic enters appreciably, although two meters show variations of about 3 per cent when the harmonic amounts to as much as 50 per cent of the fundamental.

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